

PROLOG -

the language
and its implementation
compared with Lisp

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Our Work

What?

Have implemented
a Prolog compiler (and interpreter)
for the DECsystem10 machine
(written in Prolog).

Why?

.....

The Prolog Language

- "programming in logic"
- developed by Colmerauer et al.,
 - University of Marseille
- noteworthy for:
 - fast, error-free programming
 - clear, readable, concise programs

Prolog dispenses with:

- goto
- do, for or while loops
- assignment
- references (pointers)

cf. pure Lisp

Viewpoint: Prolog as a generalisation of pure Lisp

- functions \rightarrow general procedures
- lists \rightarrow general tree structures
- function evaluation \rightarrow procedure invocation
- constructors + selectors \rightarrow pattern matching
- lambda calculus \rightarrow classical logic (subset)

Elementary Data Objects ("terms")

- "atoms"

a nil tom n1

- "integers"

0 -1 99999

- "variables"

X Y2 Jim C1

Complex Data Objects ("terms")

"functor" "arguments"
 ie. record ie. fields of the record
 -type

alternative form

point (0, 10, -10)

pair (romeo, juliet)

+ (a, b)

• (Head, Tail)

• (1, • (2, • (3, nil)))

a + b

Head • Tail

1 • 2 • 3 • nil

Procedure Call ("goal")

"predicate" "arguments"
 ie. procedure
 -name

alternative

gives (tom, apple, teacher)

reverse ((1.2.3.nil), List)

< (X, Y)

$X < Y$

Program Statements ("clauses")

interpretations

- "non-unit clause"

$P :- Q, R, S.$

P is true if Q, R and S are true.

To satisfy goal P , satisfy goals
 Q, R and S .

- "unit clause"

$P.$

P is true.

Goal P is satisfied.

- "question"

$?- P.$

Is P true?

Satisfy goal P .

Variables in Clauses

NB. The "lexical scope" of a variable is limited to a single clause.

clause

bird(X):- crow(X).

helps(X,X).

?- employs(X,X).

some possible readings

Any X is a bird if X is a crow.

To find an X which is a bird,
find an X which is a crow.

Everyone helps himself.

The goal of finding a person who
helps X is satisfied by X himself.

Does anyone employ himself?

Find an X who is self-employed.

Geographical Statistics Example

pop (china, 825).	area (china, 3380).
pop (india, 586).	area (india, 1139).
pop (ussr, 252).	area (ussr, 8708).
pop (usa, 212).	area (usa, 3609).
⋮	

density(C,D) :- pop(C,P), area(C,A), D is $(P \times 1000) / A$.

similar densities (C1,C2) :-

density(C1,D1), density(C2,D2),
 $D1 \geq D2$, $D1 \times 20 < D2 \times 21$, $C1 \neq C2$.

Using the Geographical Statistics Program

Question

Answer

- | | |
|---------------------------------------|---------------|
| ?- similar densities (france, china). | yes |
| ?- density (france, X). | X = 246 |
| ?- similar densities (X, pakistan). | X = indonesia |
| ?- similar densities (pakistan, X). | no |
| ?- similar densities (X, Y). | |

X = indonesia	Y = pakistan
X = uk	Y = w_germany
X = italy	Y = philippines
X = france	Y = china
⋮	

The Declarative Semantics of Prolog

Prolog_program

<p> $P :- Q, R.$ $P :- R, S.$ $R :- S.$ $S.$ </p>
--



its (declarative) semantics

<p> \dots $P_1.$ $P_2.$ $P_3.$ \dots $R_1.$ $R_2.$ \dots $S_1.$ $S_2.$ \dots </p>
--

The Declarative Semantics, Precisely Stated

A goal is true if it is the head of some clause instance and each of the goals (if any) in the body of that clause instance is true.

where

An instance of a clause (or term) is obtained by substituting, for each of zero or more of its variables, a new term for all occurrences of the variable.

The Procedural Semantics of Prolog

- Execute a goal by matching* it against the head of a clause and then executing the clause's body.
 - Execute goals in left-to-right order.
 - Try clauses in top-to-bottom order.
 - If a match can't be found, "backtrack".
- * Matching ("unification") finds the most general common instance of goal and clause head.

A Conventional Program for the 'similardensities' procedure

Case: ? - similardensities (C1, C2).

for C1 from 1 to N do

integer D1 := density(C1);

for C2 from 1 to N do

integer D2 := density(C2);

if D1 \geq D2 and D1 \times 20 < D2 \times 21

and C1 \neq C2

then output(C1, C2)

repeat

repeat

Concatenating Lists

Lisp:

$$\begin{aligned} \text{append}[L1; L2] = \\ & [\text{null}[L1] \rightarrow L2; \\ & T \rightarrow \text{cons}[\text{car}[L1]; \text{append}[\text{cdr}[L1]; L2]]] \end{aligned}$$

Prolog:

append(nil, L, L).

append((X.L1), L2, (X.L3)) :-
append(L1, L2, L3).

Different Uses of the 'append' Procedure

?- append((a.b.c.nil), (d.e.nil), X).

?- append(X, Y, (a.b.c.d.e.nil)).

member(X, L) :- append(L1, (X.L2), L).

Differentiating an Algebraic Expression

$$d(U+V, X, DU+DV) :- \\ d(U, X, DU), d(V, X, DV).$$

$$d(U \times V, X, DU \times V + U \times DV) :- \\ d(U, X, DU), d(V, X, DV).$$

$$d(X, X, 1).$$

$$d(C, X, 0) :- \text{atomic}(C), C \neq X.$$

The Equivalent Differentiation Procedure in Lisp

```

DERIV (LAMBDA (E X)
  (COND ((ATOM E) (COND ((EQ E X) 1) (T 0)))
        ((EQ (CAR E) (QUOTE PLUS))
         (LIST (CAR E)
               (DERIV (CADR E) X) (DERIV (CADDR E) X)))
        ((EQ (CAR E) (QUOTE TIMES))
         (LIST (QUOTE PLUS)
               (LIST (CAR E) (CADDR E) (DERIV (CADR E) X))
               (LIST (CAR E) (CADR E) (DERIV (CADDR E) X))))))

```

cf. Weissman's Lisp 1.5 Primer

Special Characteristics of Prolog – Part I

- general record structures
 - no type restrictions
 - no declaration of record types
- pattern matching – replaces selectors+constructors
- more flexible procedures
 - multiple outputs
 - multi-purpose procedures
 - generate multiple alternative results
- backtracking \equiv iteration
- "logical variable" \equiv assignment+references

Special Characteristics of Prolog - Part II

- program and data expressed the same way
- declarative semantics in addition to
the usual procedural semantics
- the procedural semantics is totally defined

Prolog supported by a practical interactive system

- Built-in procedures for
 - arithmetic
 - input-output
 - file handling
 - maintaining an in-core "database"
 - state saving
- Debugging aids
 - tracing
 - interrupts
 - on-line program amendment
- Extra operator for limiting the generation of alternatives

Some Applications of Prolog - large-scale programs

- natural language understanding Colmerauer+al.
- algebraic symbol processing Kanoui+Bergman
Bundy+al.
- architectural design Markusz
- drug design applications Darvas+Futo
- compiler writing Warren+al.

Prolog Implementations

<u>When</u>	<u>Who</u>	<u>Where</u>	<u>What</u>	<u>How</u>
1972	Roussel	Marseille	interpreter	Algol-W
1974	Battani + Meloni	"	"	Fortran
1975	Szeredi	Budapest	"	CDL (Koster)
1976	Bruynooghe	Leuven (Belgium)	"	Pascal
1976	Roberts	Waterloo (Canada)	"	360/370 assembler
1976	Warren + Pereira + Pereira	Edinburgh + Lisbon	compiler → DEC10	Prolog

Innovations in Our Implementation

- Compilation
- Storage economy (with "structure sharing")
 - conventional stack mechanism to reclaim "local" variables
 - garbage collector for "global" variables
 - "mode declarations"
- Indexing of clauses
(computed goto replaces sequence of tests)

Compiling the 'append' Procedure (first clause)

```

append(          begin
                local variables L1,L2;
                global variables X,L3;
                check term[1] is of type ".";
                X := car(term[1]);
                L1 := cdr(term[1]);
                L2 := term[2];
                term[3] := cons(X,L3);
                call append(L1,L2,L3);
                return;
                end
)

```

• (X, L1), L2, • (X,L3)):-
append(L1,L2,L3).

Compiling the 'append' Procedure (second clause)

```
append(          begin
    nil,          temporary variable L;
                if term[1] is a variable
                then term[1] :≈ nil
                else check term[1] is "nil";
    L,           L := term[2];
    L).         match (term[3], L);
                return
                end
```

Comparative Performance Data

- time ratios for compiled code on DEC10

	<u>Prolog</u>	<u>Lisp*</u>	<u>Pop-2</u>
list concatenation	1	• 64	3.8
differentiation	1	1.3	2.3
	1	1.7	3.7
	1	2.6	5.4
geographical stats	1	-	1.6

* Stanford, + NOUO option.

Conclusion I

Pattern matching is better than selectors+constructors.

- More readable.
- Faster!
 - procedure argument passing not just "red tape"
 - each component only selected once
 - all components selected in a single process
 - no reloading of index registers
 - no duplication of type checks
 - ("structure-sharing" gives faster "cons")

Conclusion II

In principle, Prolog supersedes Lisp ...

- More readable
 - smaller program units
 - less complex (nested)
 - natural declarative reading
- General record structures replace lists
- General procedures replace simple functions
- Pure Prolog provides high-level substitutes for
 - iteration
 - assignment
 - references
- Prolog is practically as efficient as Lisp